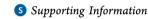




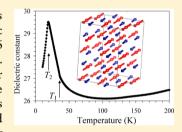
# Sc<sub>2</sub>NiMnO<sub>6</sub>: A Double-Perovskite with a Magnetodielectric Response **Driven by Multiple Magnetic Orders**

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ABSTRACT: Perovskite materials provide a large variety of interesting physical properties and applications. Here, we report on unique properties of a fully ordered magnetodielectric double-perovskite,  $Sc_2NiMnO_6$  (space group  $P2_1/n$ , a = 4.99860 Å, b = 5.35281 Å, c = 7.34496Å, and  $\beta = 90.7915^{\circ}$ ), exhibiting sequential magnetic transitions at  $T_1 = 35$  K and  $T_2 = 17$  K. The transition at  $T_1$  corresponds to a single-k antiferromagnetic phase with propagation vector  $\mathbf{k}_1 = (1/2, 0, 1/2)$ , while the second transition at  $T_2$  corresponds to a 2-k magnetic structure with propagation vectors  $\mathbf{k}_1 = (1/2, 0, 1/2)$  and  $\mathbf{k}_2 = (0, 1/2, 1/2)$ . Symmetry analysis suggests that the two ordering wave vectors are independent, and calculations imply that  $\mathbf{k}_1$  is associated with the Mn sublattice and k2 with the Ni sublattice, suggesting that Mn-Ni coupling is very



small or absent. A magnetodielectric anomaly at T<sub>2</sub> likely arises from an antiferroelectric ordering that results from the exchangestriction between the two magnetic sublattices belonging to k1 and k2. The behavior of Sc2NiMnO6 demonstrates 3d doubleperovskites with small A-site cations as a promising avenue in which to search for magnetoelectric materials.

# 1. INTRODUCTION

Magnetodielectrics, that is, materials whose dielectric properties can be controlled by a magnetic field, or alternatively, whose magnetic ordering can produce a dielectric anomaly, have attracted scientific interest owing to their merits for both fundamental research and technological applications. 1-4 Magnetodielectric (MD) effects are typically caused by spinlattice coupling<sup>4</sup> and are key to the behavior of many magnetocaloric materials and type-II multiferroics. 5,6 Nonmultiferroic magnetodielectrics can be classified into two categories: frustrated magnets such as R<sub>2</sub>Ti<sub>2</sub>O<sub>7</sub>,<sup>7,8</sup> and magnetic materials that show a dielectric anomaly in the vicinity of magnetic order such as Mn<sub>3</sub>O<sub>4</sub>,<sup>3</sup> TeCuO<sub>3</sub>,<sup>4</sup> and Dy<sub>3</sub>Fe<sub>5</sub>O<sub>12</sub>,<sup>9</sup>

The discovery and characterization of magnetodielectric materials are necessary to improve understanding of the underlying mechanisms and to optimize material properties for realistic device applications. An ideal system for such exploration is the double-perovskite structure with the formula A<sub>2</sub>BB'O<sub>6</sub> (A is an alkaline-earth or rare-earth element; B and B' are transition metals). The B and B' sites are able to accommodate various cations with different electronic configurations, allowing the engineering of superexchange pathways by appropriate choice of magnetic B and B' cations. Doubleperovskites thus display a wealth of magnetic properties including ferro-, ferri-, and antiferro-magnetism; multiferroicity; and the magnetocaloric effect, as well as spin-liquid and spinglass states.1

The double-perovskite structure is susceptible to a variety of structural instabilities, and magnetoelastic coupling of the magnetic B-site ions leads to several possible magnetostructural phase transitions. 15-21 When both B and B' are 3d metals, double-perovskites tend to be ferromagnetic (FM) insulators, and this can be understood via the Goodenough-Kanamori (G-K) rules. 22,23 Several FM double-perovskites in the Ln<sub>2</sub>CoMnO<sub>6</sub> and Ln<sub>2</sub>NiMnO<sub>6</sub> families (Ln = rare-earth elements) have been identified as having interesting magnetodielectric, magnetocaloric, or multiferroic propterties. 20,24-30 The study of the mechanisms underlying these behaviors is complicated by a great sensitivity to variations in synthesis

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conditions and in particular to the degree of B/B′ cation ordering. Synthesis of double-perovskite magnetodielectrics with antiferromagnetic (AFM) order would provide complementary knowledge about the relationship between magnetic structures and MD behavior, through insights into the role played by the magnetism. The recent synthesis of the AFM multiferroic In<sub>2</sub>NiMnO<sub>6</sub>, with a small In<sup>3+</sup> cation at the A site, 33,34 where a ferroelectric polarization of 30  $\mu$ C/m² is developed below  $T_N = 26 \text{ K}$ , 35 represents a key development in this direction. The synthesis of Sc<sub>2</sub>NiMnO<sub>6</sub> has been attempted in the literature; however, the ordered phase has not been obtained.

In this work, we report the high-pressure synthesis, structural, magnetic, and electrical properties of the AFM double-perovskite magnetodielectric,  $\operatorname{Sc_2NiMnO_6}$ , with the ordered structure. There is an AFM ordering transition at  $T_1$  = 35 K to a single-k magnetic structure (AFM I) and a second magnetic transition at  $T_2$  = 17 K to a 2-k magnetic structure (AFM II), which is accompanied by a sharp anomaly in the dielectric constant. The magnetodielectric response  $[\varepsilon(H) - \varepsilon(0)]/\varepsilon(0)$  peaks at  $T_2$  with a value of ~2.7% for H ~ 90 kOe. This behavior arises from the substantial suppression of the transition temperature  $T_2$  in response to an applied magnetic field. Neutron powder diffraction provides evidence for an unusual magnetic structure in which the Ni and Mn sublattices order independently with different wavevectors.

#### 2. EXPERIMENTAL DETAILS

 $Sc_2NiMnO_6$  was synthesized from a stoichiometric mixture of  $Sc_2O_3$  (99.99%), NiO (99.9%), and  $MnO_2$  (99.997%) by a solid-state reaction under high-pressure and high-temperature conditions. The mixture (about 0.4 g) was placed into Pt capsules and was treated at 1373–1773 K for 2 h in a press of 6 GPa in a belt-type high-pressure apparatus (Figures S1 and S2). After reaction, the samples were quenched to room temperature before the pressure was released.

Powder X-ray diffraction (XRD) data were collected at room temperature (RT) on a RIGAKU Ultima III diffractometer using Cu  $K\alpha$  radiation (2 $\theta$  range of 10-80°, a step width of 0.02°, and a counting time of 1-10 s/step). Electron probe microanalysis (EPMA) was performed on a JEOL, JXA-8500F instrument. The surface of the pellet sample was polished on a fine (0.3  $\mu$ m) alumina coated film before measurement. MnO, NiO, and Sc2O3 were used as standard samples for Mn, Ni, and Sc, respectively. The EPMA data supported the chemical composition of Sc:Ni:Mn = 2.02(4):0.96(2):1. The sample was then measured with synchrotron XRD at RT on a Debye-Scherrer camera at the BL15XU beamline of SPring-8.<sup>37</sup> The data were collected between  $2^{\circ}$  and  $60^{\circ}$  in  $2\theta$  with a step of  $0.003^{\circ}$  and an incident wavelength of 0.65297 Å. A fine powder of the sample was packed into a 0.1 mm Lindemann glass capillary which was rotated during the measurement. Obtained synchrotron XRD patterns were analyzed by the Rietveld method using the programs RIETAN-2000 and VESTA.38,39

Magnetic susceptibility ( $\chi=M/H$ ) was measured on a SQUID magnetometer (Quantum Design, MPMS) between 2 and 400 K in various magnetic fields under both zero-field-cooling (ZFC) and field-cooling (FC) conditions. Isothermal magnetization measurements were performed between -50 and 50 kOe at various temperatures on the same apparatus. <sup>57</sup>Fe Mössbauer spectra were measured at 12, 25, 45, and 300 K using a conventional constant-acceleration spectrometer. The radiation source  $^{57}$ Co/Rh was kept at RT. The obtained spectra were calibrated by  $\alpha$ -Fe as a standard and were fitted by the Lorentzian function.

Specific heat,  $C_{\rm p}$ , was measured in magnetic fields of 0, 70, and 90 kOe between 2 and 300 K on cooling by a pulse relaxation method using a commercial calorimeter (Quantum Design PPMS). Dielectric constants were measured using an Agilent E4980A LCR meter

between 10 and 300 K at frequencies between 1 kHz and 1 MHz at various magnetic fields between -90 and 90 kOe.

Neutron powder diffraction (NPD) measurements were carried out on a 3.5 g powder sample at 300, 25, and 4 K on the SPODI high-resolution diffractometer at the FRM-II facility of the Technische Universität München, Germany, and also at 300, 36, 26, and 1.5 K, and in 1 K steps between 17 and 38 K on the WISH time-of-flight diffractometer at the ISIS Facility, 40 Rutherford Appleton Laboratory, United Kingdom.

### 3. RESULTS AND DISCUSSION

The synchrotron XRD pattern of  $Sc_2NiMnO_6$  could only be fully indexed within monoclinic symmetry with lattice parameters a=4.9986 Å, b=5.3528 Å, c=7.3450 Å, and  $\beta=90.792^{\circ}$  using TREOR. The observed reflection conditions are consistent with the space group  $P2_1/n$  (No. 14, cell choice 2) similar to other  $R_2NiMnO_6$  (R = In, Y, and rare-earth elements). We used structural parameters of  $In_2NiMnO_6^{33}$  as the starting ones in the Rietveld analysis of  $Sc_2NiMnO_6$ . The refined structural parameters, R values, selected bond lengths, and bond-valence sums  $(BVS)^{42}$  are listed in Tables 1 and S1.

Table 1. Room-Temperature Structural Parameters of Sc<sub>2</sub>NiMnO<sub>6</sub> from Synchrotron X-ray Powder Diffraction Data<sup>a</sup>

site	WP	$\boldsymbol{x}$	у	z	$B(Å^2)$
Mn	2c	0.5	0	0.5	0.50(2)
Ni	2d	0.5	0	0	0.71(2)
Sc	4e	0.97474(17)	0.07530(10)	0.25372(15)	0.772(16)
O1	4e	0.3567(4)	0.9403(4)	0.2610(4)	0.81(5)
O2	4e	0.1967(5)	0.1821(5)	0.5642(3)	1.11(6)
O3	4e	0.6749(5)	0.2988(5)	0.4252(3)	1.07(6)

<sup>a</sup>WP: Wyckoff position. Space group is  $P2_1/n$  (No. 14, cell choice 2). Z=2,  $\lambda=0.65297$  Å. Full occupancy factors for all sites. a=4.99860(2) Å, b=5.35281(2) Å, c=7.34496(2) Å, β=90.7915(2)°, V=196.5068(11) ų, and ρ=5.062 g/cm³. Final R values were  $R_{\rm wp}=4.08\%$ ,  $R_{\rm p}=2.65\%$ ,  $R_{\rm B}=4.81\%$ , and  $R_{\rm F}=3.93\%$ .

The experimental, calculated, and difference patterns are shown in Figure 1. The refined crystal structure is illustrated in Figure 2. The Ni and Mn ions are alternatively located in the cornershared octahedral environments with three unique Ni–O and

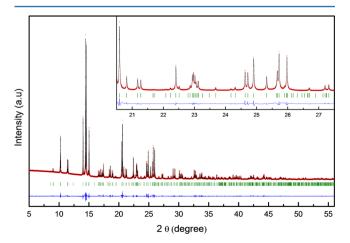


Figure 1. Observed (red), calculated (black), and difference (blue) synchrotron XRD patterns of  $Sc_2NiMnO_6$  at RT ( $\lambda=0.65297$  Å). The small tick marks denote simulated peak positions. The inset shows enlarged view of the profiles between 20.5 and 27.5° of the  $2\theta$  range.

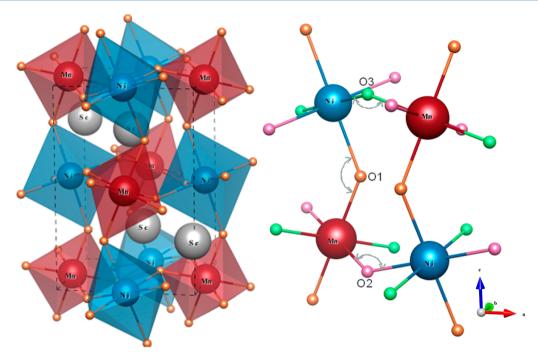
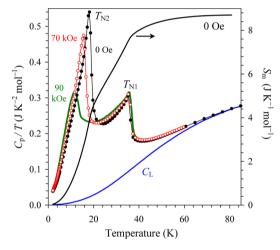


Figure 2. Crystal structure of  $Sc_2NiMnO_6$ , indicating the tilted octahedra belonging to Ni and Mn, as well as the three unique 3d-O-3d bond angles.

Mn-O distances. The BVS analysis of the metal-oxygen distances gives a valence of 4+ for Mn and 2+ for Ni. In the subsequent discussion of the NPD results, we find further evidence for the complete ordering of the Ni and Mn sites.

The lattice parameters and unit cell volume of Sc<sub>2</sub>NiMnO<sub>6</sub> are all the smallest among known R2NiMnO6 compounds with the  $P2_1/n$  space group (see Figure S3a and S3b). Moreover, Sc<sub>2</sub>NiMnO<sub>6</sub> has the smallest average Ni-O-Mn bond angle of 137.4° (Figure S3d), resulting from a significant octahedral tilting of the crystal structure (pattern a a c t in the Glazer notation<sup>43</sup>). The magnetic ground states in R<sub>2</sub>NiMnO<sub>6</sub> are often expected to be FM<sup>30,44,45</sup> within the framework of G-K rules because of the superexchange interaction between the half-filled e<sub>o</sub> orbital of Ni<sup>2+</sup> and the valence e<sub>o</sub> orbital of Mn<sup>4+</sup> bridged by the p orbital of O<sup>2-</sup>. The FM interaction strength can be gradually reduced through the decrease of the Ni-O-Mn bond angles which reduces the hopping integral, thus monotonically decreasing the FM ordering temperature (Figure S3c)<sup>44,45</sup> or even stabilizing a complex noncollinear AFM ground state in multiferroic  $In_2NiMnO_6$ .  $^{35}$   $Y_2NiMnO_6$   $(r_{VIII}(Y^{3+}) = 1.019$  Å) was predicted to be an AFM multiferroic <sup>19</sup> but was observed to be an FM insulator with  $T_{\rm C}$  of 72 K;<sup>27,44,45</sup> therefore, its reported multiferroic properties<sup>29</sup> need further verification because an FM structure does not produce ferroelectric polarization.<sup>27</sup> Up to now, only  $In_2NiMnO_6$  ( $r_{VIII}(In^{3+}) = 0.92$  Å) shows AFM behavior, suggesting that antiferromagnetism can only appear in R<sub>2</sub>NiMnO<sub>6</sub> with R ions below a critical radius<sup>33</sup> from which it is natural to suspect that the ordered state in Sc<sub>2</sub>NiMnO<sub>6</sub>  $(r_{VIII}(Sc^{3+}) = 0.870 \text{ Å})$  may also be AFM.

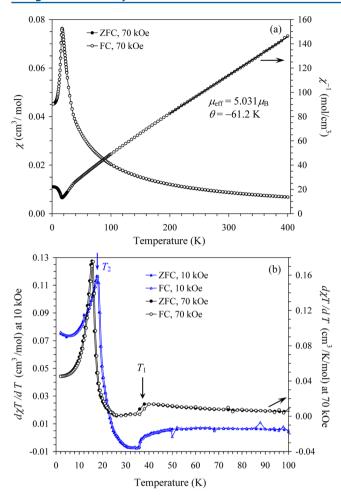
Figure 3 shows the temperature and magnetic field dependence of the specific heat capacity  $C_p$  of  $Sc_2NiMnO_6$ . Two large peaks are observed at  $T_1 = 35$  K and  $T_2 = 17$  K, corresponding to two phase transitions that are bulk in nature. A magnetic field has a negligible effect on the transition at  $T_1$ , whereas a moderate magnetic field reduces  $T_2$  by approximately



**Figure 3.** Heat capacity  $C_p(T)$  of  $Sc_2NiMnO_6$  in the form of  $C_p/T$  vs T between 2 and 84 K at various H. (The molecular weight is calculated for the ABO $_3$  composition.) The thin blue line shows the lattice contribution (from  $ScRhO_3$ ). The right-hand axis gives the temperature dependence of magnetic entropy.

1 K/Tesla. The lattice contribution ( $C_{\rm L}$ ) to the total specific heat  $C_{\rm p}$  was estimated by using the data of nonmagnetic ScRhO<sub>3</sub>,<sup>46</sup> that is,  $C_{\rm L} = C_{\rm p}({\rm ScRhO_3})$  (Figure S4). The magnetic contribution ( $C_{\rm M}$ ) was thus obtained through  $C_{\rm M}({\rm ScNi_{0.5}Mn_{0.5}O_3}) = C_{\rm p}({\rm ScNi_{0.5}Mn_{0.5}O_3}) - C_{\rm L}$ . The magnetic entropy was obtained using the thermodynamic relationship  $S_{\rm m} = \int (C_{\rm m}/T) {\rm d}T$ . The entropy associated with the phase transitions is found to be about 17.4 J K<sup>-1</sup> mol<sup>-1</sup> (for Sc<sub>2</sub>NiMnO<sub>6</sub>), more than 84% of the expected value, 20.7 J K<sup>-1</sup> mol<sup>-1</sup>, suggesting most of the entropy is removed. Because  $T_{\rm 1}$  and  $T_{\rm 2}$  are close, it is very difficult to unambiguously estimate the entropy at each transition.

The temperature-dependent magnetic susceptibility ( $\chi$  vs T) of Sc<sub>2</sub>NiMnO<sub>6</sub> is presented in Figure 4 (top). ZFC and FC



**Figure 4.** Top: Temperature dependence of  $\chi$  for Sc<sub>2</sub>NiMnO<sub>6</sub> at H = 70 kOe. The right-hand axis gives the reciprocal  $\chi^{-1}$  with the Curie–Weiss fit (solid line). Bottom: Temperature dependence of  $\chi$  in a form  $d\chi T/dT$  vs T at 10 kOe (left-hand axis) and 70 kOe (right-hand axis).

curves are virtually indistinguishable, and a sharp peak is visible at  $T_2 = 17$  K in both. A plot of  $\chi^{-1}$  versus T was fit to a Curie— Weiss (CW) law, shown by the solid curve. A least-squares fit to the paramagnetic range between 200 and 400 K yielded  $\theta_{\mathrm{CW}}$ = -61.2(7) K and  $\mu_{\text{eff}} = 5.031(5)\mu_{\text{B}}/\text{f.u.}$  (f.u. is formula unit); these values were independent of the measuring field H. The negative  $\theta_{\rm CW}$  indicates dominant AFM interactions, consistent with the magnetic structure results presented later. The measured  $\mu_{\rm eff}$  is close to that of In<sub>2</sub>NiMnO<sub>6</sub> ( $\mu_{\rm eff}$  = 4.891 $\mu_{\rm B}$ )<sup>33</sup> and to the expected value of 4.796  $\mu_{\rm B}$ /f.u. for  $Sc_2NiMnO_6$  with one  $Mn^{4+}$  (S=3/2) and one  $Ni^{2+}$  (S=1). Although no obvious anomalies appear at other temperatures, the reciprocal  $\chi^{-1}$  versus T curve shows a kink at  $T_1 = 35$  K, seen in Figure 4 (top), which can be more easily observed in the  $d\chi T/dT$  versus T curves of Figure 4 (bottom). The linear M versus H dependence of the isothermal magnetization measured at 2 K (Figure S5) indicates that the ground state is a fully compensated antiferromagnet.

The magnetic nature of the two transitions was confirmed by Mössbauer spectroscopy of Sc<sub>2</sub>NiMnO<sub>6</sub>:0.5%<sup>57</sup>Fe (Figure 5). Spectra above  $T_1$  (at 300 and 45 K) consist of paramagnetic doublets, Fe1 and Fe2, with different isomer shifts ( $\delta_{\rm Fe1}$  = 0.35(1) and  $\delta_{\rm Fe2}$  = 0.42(1) mm/s, at 300 K) and quadrupole splittings ( $\Delta_{\rm Fe1}$  = 0.56(2) and  $\Delta_{\rm Fe2}$  = 1.38(1) mm/s). From our investigation of several ScMO<sub>3</sub> and InMO<sub>3</sub> perovskites with M

= 3d transition metals, 47 we found that the Fe1 and Fe2 doublets originate from <sup>57</sup>Fe<sup>3+</sup> cations located in the B and A sublattices of the perovskite structure, respectively. For Sc<sub>2</sub>NiMnO<sub>6</sub>:0.5%<sup>57</sup>Fe, it means that a small amount of <sup>57</sup>Fe<sup>3+</sup> cations is located at the Sc site. The Fe2 contribution (from the Sc sublattice) is not important for our discussion. Spectra at 25 K (between  $T_1$  and  $T_2$ ) have two hyperfine magnetic contributions: the first subspectrum, Fe1<sub>m</sub>, is a well-defined six-line Zeeman sextet, and the second subspectrum, Fe2<sub>m</sub>, has a continuous distribution of hyperfine magnetic field. The distribution of internal fields for  $Fe2_m$  extends to zero (Figure 5d), indicating that some of the  $^{57}Fe^{3+}$  ions are not subject to any static magnetic fields. The Mössbauer spectra between  $T_1$ and T2 suggest quite different magnetic environments of the <sup>57</sup>Fe<sup>3+</sup> cations at the Mn and Ni sites, although a priori it cannot be determined which signal belongs to which site. On the basis of further considerations (see later text), we interpret the welldefined Zeeman sextet as originating from 57Fe3+ cations located at the Mn site. Below  $T_2$  (at 12 K), the distribution function for the Fe2<sub>m</sub> subspectrum changes from continuous to discrete, indicating the onset of long-range ordering in both sublattices.

The frequency-dependent dielectric constant of  $Sc_2NiMnO_6$  is shown in Figures 6 and S8 as a function of temperature,  $\varepsilon(T)$ . The curves start to increase more rapidly on lowering temperature below  $T_1$  until reaching a maximum at  $T_2$ , below which the  $\varepsilon(T)$  curves drop rapidly. In contrast to the  $\varepsilon(T)$  of compounds such as  $LnMnO_3$  (Ln = Y and Ho-Lu),  $^{48,49}$  no temperature hysteresis is visible during cooling and warming.

The  $\varepsilon(T)$  curves in applied magnetic fields of up to 90 kOe at a fixed frequency of 46.4 kHz are shown in Figure 7a. The peak in  $\varepsilon(T)$  is sensitive to H, shifting from  $\sim$ 17 K at H=0 to 12.5 K at H=90 kOe in the same manner as the ordering temperature determined from the heat capacity. The MD ratio  $\varepsilon_{\text{MD}}(H)$ , defined as  $\varepsilon_{\text{MD}}=[\varepsilon(H)-\varepsilon(0)]/\varepsilon(0)\times 100\%]$ , is plotted in Figure 7b, and its behavior can be understood from the large sensitivity of  $T_2$  to an applied field. Just above 18 K,  $\varepsilon_{\text{MD}}(H)$  is negative owing to the suppression of the peak in  $\varepsilon$  at  $T_2$ , while below 18 K,  $\varepsilon_{\text{MD}}(H)$  increases until  $T_2$  is coincident with the temperature, after which  $\varepsilon_{\text{MD}}(H)$  decreases rapidly.

We also attempted to measure the electric polarization as a function of temperature and found no evidence for any pyroelectric current, demonstrating that the dielectric anomaly is not due to a ferroelectric transition. The anomaly could be attributed to antiferroelectric behavior as is observed in some double-perovskites with the formula  $Pb_2MM'O_6$  (M=Mg,Co,Ni,Zn,Sc, and Fe;M'=Ti,Zr,Nb,Ta, and  $W)^{S0,S1}$  because of an order–disorder transition of the local structure. There are also cases where antiferroelectric distortions arise from magnetoelastic coupling associated with a magnetic phase transition.  $^{52}$ 

The results of the crystal structure refinement against the neutron diffraction data (Figure 8, Table 2) are fully consistent with the synchrotron XRD results above. The opposite signs of the neutron scattering lengths  $b(\mathrm{Mn})$  and  $b(\mathrm{Ni})$  allow a robust determination of the degree of B-site ordering, which is found to be 100(4)%. New diffraction peaks appear in the phase below  $T_1 = 35$  K, which we label AFM I. These peaks can be indexed with the propagation vector  $\mathbf{k}_1 = (1/2, 0, 1/2)$ . Additional peaks appear below 17 K (AFM II) which can be indexed by the propagation vector  $\mathbf{k}_2 = (0, 1/2, 1/2)$ , and these peaks coexist with the peaks belonging to  $\mathbf{k}_1$  together forming a 2-k magnetic structure. Rietveld refinement of the diffraction

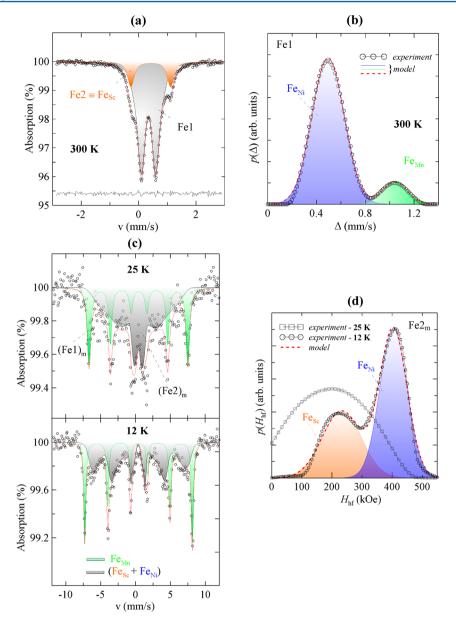
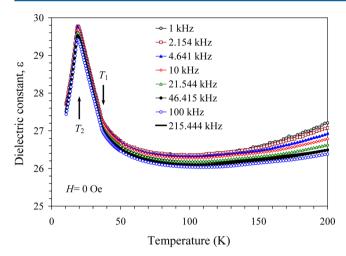


Figure 5.  $^{57}$ Fe Mössbauer spectra of Sc<sub>2</sub>NiMnO<sub>6</sub>:0.5% $^{57}$ Fe (experimental data are white symbols) at (a) 300 K and (c) 25 and 12 K and fitting results. (b) Distribution,  $p(\Delta_{Fe1})$ , of the quadrupole splitting,  $\Delta_{Fe1}$ , for the Fe1 doublet on the panel a. (d) Distribution,  $p(H_{hf})$ , of hyperfine magnetic fields,  $H_{hf}$  for the Fe2<sub>m</sub> subspectrum at 12 and 25 K from the panel c.

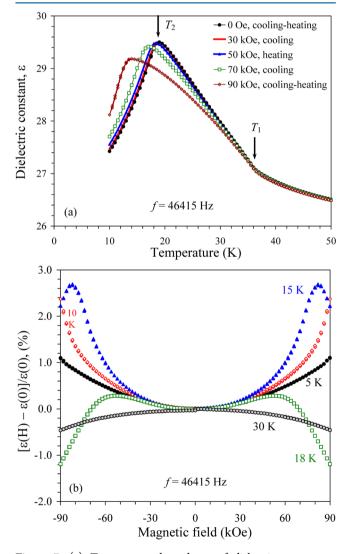
pattern was performed with the FullProf software, 53 symmetry analysis was performed with both the Basireps and ISODISTORT packages. 54,55 The space group  $P2_1/n$  has only one magnetic irreducible representation (irrep) associated with  $k_2 = (0, 1/2, 1/2)$  which is the 1-D complex representation mD1-D2-. There are four different magnetic irreps associated with  $k_1$  = (1/2, 0, 1/2) which are the 1-D irreps mY1+, mY2+, mY1-, and mY2-. The Y1± and Y2± type representations enforce a specific relation between the magnetic moments on the two equivalent Mn/Ni sites where either the xand z components of the magnetic moment change sign or only the y component changes sign. The mYn+(mYn-) type representations, importantly, specify a magnetic order on only the Mn (Ni) sublattice, a consequence of the different behavior of these sites under the inversion operation. Energetically, it is difficult to understand why the two sublattices would not order coincidently unless the Ni-O-Mn superexchange was either highly frustrated or suppressed, in which case the system might

naturally select a magnetic ordering wavevector which produces a vanishing molecular field at the site of the other transition-metal ion. A phase transition involving both the Ni and Mn irreps would remove the inversion center, reducing the space group symmetry to either  $P2_1$  or Pn and allowing ferroelectricity. However, there is no measurable anomaly in the lattice parameters associated with AFM I (Figure S9), nor is there a substantial dielectric anomaly until  $T_2$  (associated with the second phase, AFM II), both of which would be anticipated in the case of a ferroelectric phase transition. Therefore, the combined evidence from neutron diffraction and the dielectric response strongly suggests that the spins on the Mn and Ni sites order independently. Mössbauer measurements give a further support for this conclusion.

Given that the spins on the two transition-metal sublattices (Mn and Ni) order independently, it remains to identify which sublattice orders with which propagation vector,  $\mathbf{k}_1$  or  $\mathbf{k}_2$ . This information cannot be determined from the diffraction data.



**Figure 6.** Temperature dependence of dielectric constant of  $Sc_2NiMnO_6$  at various frequencies. The vertical arrows show the magnetic transition temperatures  $T_1$  and  $T_2$ .



**Figure 7.** (a) Temperature dependence of dielectric constant at various magnetic fields of  $Sc_2NiMnO_6$  at fixed frequency of  $f=46\,415$  Hz. (b) The H dependence of  $\varepsilon_{\rm MD}$  of  $Sc_2NiMnO_6$  at various temperatures and fixed  $f=46\,415$  Hz.

Instead, we have used a mean-field Heisenberg model to analyze the stability of the magnetic structures and have calculated the dominant Ni–O–O–Ni and Mn–O–O–Mn extended superexchange interactions using the CAESAR program<sup>57</sup> (see Figure S10). The  $\mathbf{k}_1$  magnetic structure requires a dominant AFM interaction between equivalent sites separated by a distance a along the a axis, and the CAESAR calculations show that this condition applies to the Mn sublattice but not to the Ni sublattice. Hence, we infer that it is the Mn spins which order at  $T_1 = 35$  K with propagation vector  $\mathbf{k}_1$ , and the Ni spins order at  $T_2 = 17$  K with propagation vector  $\mathbf{k}_2$ .

To refine the details of the magnetic structures further, we first fitted the paramagnetic phase with data from banks 2 through 9 of the WISH instrument in order to accurately determine the instrument and structural parameters. Below  $T_1$ , we fixed the instrumental parameters and fitted only the background, atomic coordinates, lattice parameters, isotropic thermal displacements, absorption, and scale. We fitted the magnetic data only from banks 2 and 9, which contain the most information on the magnetic structure as they capture the largest d-spacings, and from these two banks, we subtract the high-temperature data to obtain only the magnetic peaks. For the AFM I phase, we allowed the components of the Mn moment  $(M_a, M_b, M_c)$  to freely refine, and we obtained excellent agreement with the data with the parameters found in Table 2. For the AFM II phase, we refined a magnetic moment on the Ni site in addition to that on the Mn site. For the fit to converge, it was necessary to fix the  $M_h$ -component of the Ni magnetic moment to be zero. The magnetic peak widths for this phase are broader, indicating a shorter correlation length for the Ni sublattice and necessitating the free refinement of the associated peak-width parameters. The results of the refinement at 1.5 K are tabulated in Table 2, and the refined structures are shown in Figure 9. The combination of two k-vectors and two active irreps below  $T_2$  is compatible with a magnetostrictive antiferroelectric effect which would be capable of producing the observed dielectric anomaly.

The two AFM ordered states detailed above are both unusual for a double perovskite lattice with 3d ions on the B-sites. For example, the Ni-O-Mn nearest-neighbor exchange is expected to be FM according to the G-K rules, and deviations from this are commonly a result of coupling between a 3d cation and either a 4d or 5d cation such as in Sr<sub>2</sub>CoOsO<sub>6</sub>. 13 After In<sub>2</sub>NiMnO<sub>6</sub>, Sc<sub>2</sub>NiMnO<sub>6</sub> is only the second B-site-ordered double perovskite in the R<sub>2</sub>BB'O<sub>6</sub> family, where both B and B' are 3d metals, to show AFM order. This can be partially understood from results on the R<sub>2</sub>NiMnO<sub>6</sub> series, where the increased octahedral tilting associated with decreasing A-site cation radius is a key ingredient in suppressing the FM nearest neighbor (FM-NN) exchange (Figure S3). However, the ordering vector  $\mathbf{k_1} = (1/2, 0, 1/2)$  (which has not, to our knowledge, been reported in any other double perovskites containing 3d ions at the B and B' sites) is particularly notable here as it produces no molecular field at the sites of the Ni atoms, alleviating the competition between FM-NN and AFM-NNN superexchanges. Moreover, the occurrence of two separate magnetic phase transitions, apparently associated with the independent ordering of the two 3d ions, appears to be unique among all known oxides and is surprising given the near ubiquity of ferromagnetism in similar materials driven by FM Ni-O-Mn superexchange.

From the results obtained for  $Sc_2NiMnO_6$ , a schematic magnetic phase diagram of the  $R_2NiMnO_6$  family (R =  $Sc_7$  In,

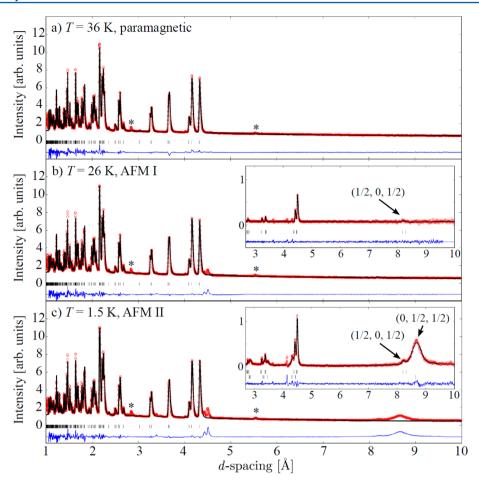


Figure 8. Neutron powder patterns merged from banks 2 and 9 on WISH recorded in (a) the paramagnetic phase, (b) AFM I, and (c) AFM II. Observed (red), calculated (black), and difference (blue) profiles. Asterisks mark a small amount (<5%) of  $Sc_2O_3$  impurity. The magnetic-only diffraction patterns, with the nuclear peaks subtracted, are shown in the insets. The refinements in the main panels include the nuclear contributions only. The small tick marks denote simulated peak positions for the corresponding contributions.

Table 2. Refined Values of the Crystal and Magnetic Structures from the 2nd and 9th Banks of WISH at 1.5 K

site	$\boldsymbol{x}$	y	z	$B(Å^2)$
Mn	0.5	0	0.5	0.89(99)
Ni	0.5	0	0	0.29(67)
Sc	0.973(1)	0.077(1)	0.254(1)	2.56(61)
O1	0.366(2)	0.938(3)	0.258(2)	1.09(69)
O2	0.192(3)	0.184(3)	0.563(2)	1.07(76)
O3	0.674(3)	0.300 (3)	0.426(2)	0.86(71)
site	$M_a$	$M_b$	$M_c$	k-vector
Mn	1.17(18)	-0.01(1)	1.19(23)	(1/2,0,1/2)
Ni	-1.03(42)	0 (-)	-1.09(27)	(0,1/2,1/2)

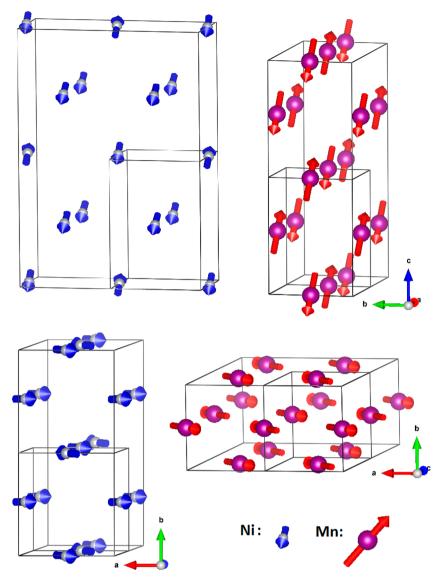
Space group  $P2_1/n$ , lattice constants a = 4.99086(5) Å, b = 5.35269(6) Å, c = 7.34122(8) Å,  $\beta = 90.869(1)^{\circ}$ . Final R values for the 1.5 K pattern were  $R_{\rm Bragg} = 4.6\%$ ,  $R_{\rm mag}$  (Mn) = 3.13%, and  $R_{\rm mag}$  (Ni) = 2.37%.

Y, and rare-earth elements) with the ordered  $P2_1/n$  structure can be constructed (Figure 10). This phase diagram resembles, to some extent, a magnetic phase diagram of LnMnO<sub>3</sub>, where complex noncollinear magnetic structures are sandwiched between basically collinear magnetic structures of the A-type (with a small spin canting) and E-type. In  $R_2$ NiMnO<sub>6</sub>, a complex noncollinear magnetic structure found in

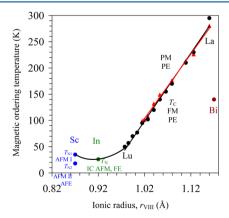
 $In_2NiMnO_6^{35}$  is sandwiched between FM (with a small canting)<sup>30</sup> and AFM collinear magnetic structures.

### CONCLUSION

Sc<sub>2</sub>NiMnO<sub>6</sub> has been successfully synthesized by a highpressure method and has been found to have the roomtemperature space group  $P2_1/n$ . Below  $T_1 = 35$  K, the material orders antiferromagnetically with a propagation vector  $\mathbf{k}_1 = (1/$ 2, 0, 1/2), while below  $T_2 = 17$  K an additional AFM component with a propagation vector of  $\mathbf{k}_2 = (0, 1/2, 1/2)$ appears. We have presented a model which describes a unique scenario whereby the Mn ions order at  $T_1$  with  $\mathbf{k}_1$ , and the Ni ions order at  $T_2$  with  $k_2$ . This would imply that nearestneighbor superexchange between Ni and Mn is heavily suppressed compared to the next-nearest-neighbor Ni-Ni and Mn-Mn extended superexchanges. The dielectric anomaly onsets only in response to the second magnetic ordering, that is, when both sublattices are magnetically ordered, which could be explained by the onset of antiferroelectricity in response to an intersublattice magnetostriction. The magnetic field dependence of the dielectric anomaly is yet to be fully understood. These results suggest that small A-site cations in B-site-ordered double perovskites of magnetic 3d ions represent an interesting playground for the exploration of magnetoelectric phenomena.



**Figure 9.** Refined magnetic structure (in phase AFM II), with the blue arrows as the Ni<sup>2+</sup> moments and the Mn<sup>4+</sup> moments in red. The moments lie primarily in the *ac*-plane at an angle of almost 45° to the *a*-axis. A nuclear cell is  $^{1}/_{8}$  of the total magnetic cell. The figure is produced using VESTA.<sup>39</sup>



**Figure 10.** Magnetic phase diagram of the R<sub>2</sub>NiMnO<sub>6</sub> family (R = Sc, In, Y, and rare-earth elements) with the ordered  $P2_1/n$  structure. <sup>33,35,45</sup> PM, paramagnetic; FM, ferromagnetic; AFM, (collinear) antiferromagnetic; IC AFM, incommensurate antiferromagnetic;  $T_{\rm N}$ , the AFM Neel temperature;  $T_{\rm C}$  the FM Curie temperature; PE, paraelectric; FE, ferroelectric; AFE, antiferroelectric.  $T_{\rm C}$  of Bi<sub>2</sub>NiMnO<sub>6</sub>, crystallizing in a different structure, <sup>15</sup> is shown for comparison.

# ASSOCIATED CONTENT

# **S** Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.inorg-chem.5b01195.

Partial refined crystal structure details, isothermal magnetizations, detailed discussion of the Mössbauer spectra, and the details of specific heat and magnetic results and the mean-field analysis and CAESAR calculation (PDF)

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# **Author Contributions**

W. Yi and A. J. Princep contributed equally to this work. All authors have given approval to the final version.

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#### Notes

The authors declare no competing financial interest.

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